

Formulas of electrotechnic and electronic

Cross-section for **single wire round**

$$q = \frac{D^2 \cdot \pi}{4} \text{ or } D^2 \cdot 0,7854$$

Cross-section for **bunched wire**

$$q = \frac{d^2 \cdot \pi}{4} \cdot n \text{ or } d^2 \cdot 0,7854 \cdot n$$

Diameter for

single wires cross-section

$$D = \sqrt{\frac{q \cdot 4}{\pi}} \text{ or } \sqrt{q \cdot 1,2732}$$

Diameter for **bunched wires**

$$D = \sqrt{1,34 \cdot n \cdot d}$$

q = cross-section(mm²)

D = conductor diameter (mm)

d = single wire diameter (mm)

n = number of wires

Conductor Resistance

$$R = \frac{l}{\kappa \cdot q} \text{ oder } \frac{\rho \cdot l}{q}$$

$$R_{\text{Schleife}} = \frac{2 \cdot l}{\kappa \cdot q} \text{ oder } \frac{2 \cdot l \cdot \rho}{q}$$

R = Electrical direct-current resistant (Ohm)

R_{Schleife} = Resistance of a complete circuit

q = cross-section (mm² or q mm)

κ (Kappa) = Conductivity

ρ (Rho) = Specific resistance ($\rho = \frac{1}{\kappa}$)

l = Conductor length (m)

| Materials | Conductivity $\frac{m}{\Omega \cdot mm^2}$ | Spec. resistance $\frac{\Omega \cdot mm^2}{m}$ |
|------------|---|---|
| Copper | 58,00 | 0,01724 |
| Aluminium | 33,00 | 0,0303 |
| Silver | 62,00 | 0,1613 |
| Iron | 7,70 | 0,1299 |
| Constantan | 2,00 | 0,50 |

Serial connection

$$\text{Resistance: } R = R_1 + R_2 + R_3 + \dots + R_n$$

$$\text{Capacitance: } \frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} + \dots + \frac{1}{C_n}$$

$$\text{Inductance: } L = L_1 + L_2 + L_3 + \dots + L_n$$

Parallel connection

$$\text{Resistance: } R = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots + \frac{1}{R_n}}$$

$$\text{Capacitance: } C = C_1 + C_2 + C_3 + \dots + C_n$$

$$\text{Inductance: } L = \frac{1}{\frac{1}{L_1} + \frac{1}{L_2} + \frac{1}{L_3} + \dots + \frac{1}{L_n}}$$

Equivalent resistance of 2 parallel connected resistance

$$R = \frac{R_1 \cdot R_2}{R_1 + R_2}$$

Mutual capacity (C)

• coaxial cable $C = \frac{\xi r \cdot 10^3}{18 \cdot \ln \frac{D_a}{d}}$ (nF/km)

• parallel core $C = \frac{\xi r \cdot 10^3}{36 \cdot \ln \frac{D_a}{d}}$ (nF/km)

• shielded twisted pair

$$C_B = \frac{\xi r \cdot 10^3}{36 \ln \frac{2a}{d} \cdot \frac{(D_a^2 - a^2)}{(D_a^2 - d^2)}} \text{ (nF/km)}$$

Da = Outer diameter over insulation

Ds = diameter over shield

d = diameter of conductor

a = distance - mid to mid of both conductors

ξ = dielectric constant

Ohm's Law

The current intensity (I) is proportional to voltage (U) and inversely proportional to resistance (R)

$$I = \frac{U}{R} \quad R = \frac{U}{I} \quad U = I \cdot R$$

I = current intensity (Amps - A)

R = electrical resistance (Ω)

U = electrical voltage (V)

Conductance

$$G = \frac{1}{R} \quad 1S = \frac{1}{1 \Omega} \quad \text{or} \quad 1 \mu S = \frac{1}{1 M \Omega}$$

S (Siemens) = reziprocal value of a resistance

is used as **conductance**

1 Siemens = 1/Ohm

G = electrical conductance

Capacitance

• Single core against earth

$$C_B = \frac{\xi r \cdot 10^3}{18 \ln \frac{D_i}{d}} \text{ (nF/km or pF/m)}$$

• Unshielded symmetrical twisted pair

$$C_B = \frac{\xi r \cdot 10^3}{36 \ln \frac{2a}{d}} \text{ (nF/km or pF/m)}$$

• Coaxial pair

$$C_B = \frac{\xi r \cdot 10^3}{18 \ln \frac{D_i}{d}} \text{ (nF/km or pF/m)}$$

• Shielded symmetrical twisted pair

$$C_B = \frac{\xi r \cdot 10^3}{36 \ln \frac{2a}{d} \cdot \frac{(D_a^2 - a^2)}{(D_a^2 - d^2)}} \text{ (nF/km or pF/m)}$$

Di = outer diameter over single core (mm)

Da = outer diameter of multicores (mm)

d = conductor diameter (mm)

a = distance between two conductors mid to mid of both conductors

Inductance of parallel cores

at low frequencies

$$L = 0,4 \left(\ln \frac{D_a}{r} + 0,25 \right) \text{ mH/km}$$

at high frequencies

$$L = 0,4 \left(\ln \frac{D_a}{r} + 0 \right) \text{ mH/km}$$

Inductance of coaxial cable

at high frequencies

$$L = 0,2 \left(\ln \frac{D_a}{r} + 0 \right) \text{ mH/km}$$

Da = distance between two conductors mid to mid of both conductors

r = radius of a conductor

ξr = dielectric constant

Impedance (Z)

$$\text{for coaxial cable } Z = \frac{60}{\sqrt{\xi r}} \cdot \ln \frac{D}{d} \text{ (}\Omega\text{)}$$

D = diameter over insulation

d = conductor diameter

for communication cable

$$\text{at low frequencies } Z = \sqrt{\frac{R}{\omega C}} \text{ (}\Omega\text{)} \cdot \tan \varphi = 1, \quad \varphi = 45^\circ$$

$$\text{at high frequencies } Z = \sqrt{\frac{L}{C}} \text{ (}\Omega\text{)}$$

R = Resistance (Ω/km)

L = Inductance (mH/km)

C = Capacitance (nF/km)

ω = 2 π f

Wave length $\lambda = \frac{V}{f}$

λ = wave length

V = propagation velocity

(velocity of light: 300 000 km/s)

f = frequency

units of attenuation - Neper (N), decibel (dB) and Bel (B)

1 Np = 8,686 dB

1 dB = 0,1151 Np = $\frac{1}{10}$ Bel

1 Bel = 10 dB = 1,1513 Np